

A. Assume Dolly Nogood is a grade-school student who has a monthly allowance ($I =$ income) for recess snacks of \$20. In all of the questions below, assume S is the vertical axis variable and $I = \$20$. She is deciding how to spend her income on $S =$ cans of soda pop and $C =$ candy bars for which her utility function is given as $U = S^{1/2}C^{1/2}$. The price of $S = \$1.00$ and the price of $C = \$1.00$.

A1. If Dolly consumes $S = 10$, how much C at a maximum can she consume? What level of utility is Dolly achieving and what is her MRS (soda for candy) at that point?

$$20 = 1S + 1C \Rightarrow C = 20 - S \Rightarrow C = 20 - 10 = 10 = \text{Max } C$$

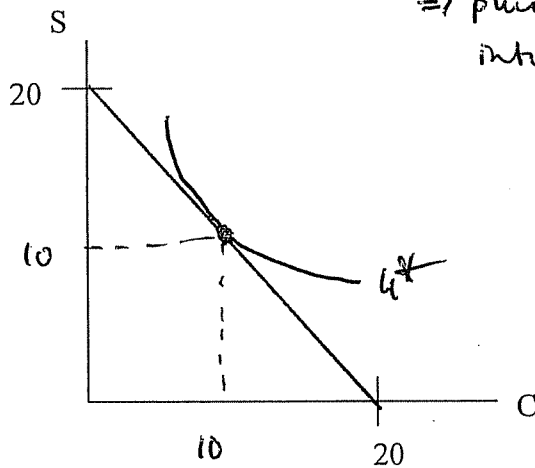
$$U = S^{1/2}C^{1/2} = (10)^{1/2}(10)^{1/2} = 10^1 = 10 = U$$

$$MRS = \frac{MU_C}{MU_S} = \frac{1/2 S^{1/2} C^{-1/2}}{1/2 C^{1/2} S^{-1/2}} = \frac{S}{C} = \frac{10}{10} = 1 = MRS$$

A2. Show Dolly's 'equal slopes condition' for maximizing her utility is $C = S$

$$\Rightarrow \frac{MU_C}{MU_S} = \frac{P_C}{P_S} \Rightarrow \frac{S}{C} = \frac{1.00}{1.00} \Rightarrow S = C \text{ or } C = S$$

A3. Show mathematically and graphically (in graph below), the attainable quantities of S and C that will maximize Dolly's utility?



\Rightarrow plug equal slopes condition into budget equation

$$\Rightarrow 20 = S + C$$

$$\Rightarrow 20 = C + C$$

$$\Rightarrow 2C = 20$$

$$\Rightarrow C = 10$$

$$\Rightarrow S = C = 10$$

B. Assume Dolly is not going to buy soda and candy but instead she is deciding how to spend her income on S = cans of soda and P = bags of popcorn for which her utility function is given by $U = \min [10S, 10P]$. The price of $S = \$1.00$ and the price of $P = \$1.00$.

B1. What attainable quantities of S and P will maximize Dolly's utility?

= pt of intersection betw budget line and pts where $10S = 10P$
 $\Rightarrow S = P$

$$20 = 1S + 1P \Rightarrow 20 = 1S + 1S \Rightarrow 2S = 20 \Rightarrow S = 10$$

B2. Show your answer to B1 in the graph below.

$$\Rightarrow P = 10$$

