

# Empirical Validation Issues for Agent-Based Computational Economics

---

**Presenter:**

**Leigh Tesfatsion**

Professor of Economics and Mathematics

Department of Economics

Iowa State University

Ames, Iowa 50011-1070

<http://www.econ.iastate.edu/tesfatsi/>

[tesfatsi@iastate.edu](mailto:tesfatsi@iastate.edu)

# Outline

---

- \* Redux: Three strands of ACE Research
- \* For which strand(s) is empirical validation appropriate?
- \* Does one approach work for all?
- \* Summary of arguments and open issues from Fagiolo, Windrum, and Moneta (2006)
- \* Other important issues related to the empirical validation of ACE models

# Three Strands of ACE Research

---

- ▣ **Qualitative Insight/Theory Generation**  
(e.g. coordination in decentralized markets,...)
- ▣ **Empirical Understanding**  
(e.g. possible reasons for empirical regularities,...)
- ▣ **Normative Understanding**  
(e.g. institutional design,...)

# ACE and Qualitative Analysis

**Illustrative Issue:** What are the performance capabilities of decentralized markets? (*Adam Smith, F. Hayek, ...*)

## **ACE Approach:**

- ◆ Construct an *agent-based world* qualitatively capturing key aspects of decentralized market economies (firms, consumers, limited information, ...)
- ◆ *Introduce traders with endowments, needs, wants, ...*  
Let the world evolve. Observe the degree of coordination that results.

**EXAMPLES:** Decentralized exchange economies without a Walrasian Auctioneer, ZI agent double-auction markets, ...

# ACE and Empirical Regularities

---

**Key Issue:** Is there a causal explanation for persistently observed empirical regularities?

## ACE Approach:

- ◆ Construct an *agent-based world* capturing salient aspects of the empirical situation.
- ◆ Investigate whether the empirical regularities can be *reliably generated* as outcomes in this world.

**Example:** ACE financial market research seeking explanation of several "stylized facts" in combination  
[www.econ.iastate.edu/tesfatsi/afinance.htm](http://www.econ.iastate.edu/tesfatsi/afinance.htm)

# ACE and Institutional Design

**Key Issue:** Does an institutional design ensure efficient, fair, and orderly social outcomes over time despite possible attempts by participants to “game” the design for their own personal advantage?

## ACE Approach:

- ◆ Construct an *agent-based world* capturing salient aspects of the institutional design.
- ◆ *Introduce agents with endowments, needs, goals, beliefs, etc.* Let the world evolve. Observe and evaluate resulting social outcomes.

**EXAMPLES:** Design of matching mechanisms, unemployment benefit programs, electricity markets

# Key Distinctions in Approaches to the Empirical Validation of ACE Models

---

- **Descriptive output validation**, i.e., matching computationally generated output against already-acquired real-world system data.
- **Predictive output validation**, i.e., matching computationally generated output against yet-to-be-acquired real-world system data.
- **Input validation**, i.e., ensuring that the structural conditions, institutional arrangements, and behavioral dispositions incorporated into a model capture the salient aspects of a real-world system under study.

# Empirical Validation of Agent-Based Models

---

**Giorgio Fagiolo**

University of Verona, Italy

Sant'Anna School of Advanced Studies, Pisa, Italy

<https://mail.sssup.it/~fagiolo>

**Alessio Moneta**

Sant'Anna School of Advanced Studies, Pisa, Italy

**Paul Windrum**

Manchester Metropolitan University Business School, Manchester, U.K.

MERIT, University of Maastricht, The Netherlands

***ACEPOL 2005***

**International Workshop on 'Agent-Based Models for Economic Policy Design'**

**Bielefeld, July 2005**



# Empirical Validation in Neo-Classical Models

---

# Empirical Validation in Neo-Classical Models

---

- A lot of different, competing approaches do exist...
  - Haavelmo-Cowles (1944) Approach
  - Structural Modeling Approach (Hansen and Sargent, 1980)
  - VAR Approach (Sims, 1980)
  - Calibration Approach (Kydland and Prescott, 1982)
  - LSE Approach (Hendry, 1988)

# Empirical Validation in Neo-Classical Models

---

- A lot of different, competing approaches do exist...
  - Haavelmo-Cowles (1944) Approach
  - Structural Modeling Approach (Hansen and Sargent, 1980)
  - VAR Approach (Sims, 1980)
  - Calibration Approach (Kydland and Prescott, 1982)
  - LSE Approach (Hendry, 1988)
  
- **Some remarks on validation approaches in NCM ...**
  - Validation is not employed to assess empirical validity of “core” theoretical assumptions (as often happens also in ABMs)
  - Heterogeneity of approaches partly reflects the open debate on validation in “philosophy of economics” (J.S. Mill; Friedman; Hutchinson, Blaug; McKloskey, Mirowski; Lawson, Mäki; etc.)

# Hot Issues in Empirical Validation of ABMs

---

# Hot Issues in Empirical Validation of ABMs

---

- Treatment of initial conditions and parameters
  - How can we deal with all “possible worlds”?

# Hot Issues in Empirical Validation of ABMs

---

- Treatment of initial conditions and parameters
  - How can we deal with all “possible worlds”?
- Comparing ABMs’ outputs and real-world observations
  - Simulated Distributions vs. Unique Real-World Observations

# Hot Issues in Empirical Validation of ABMs

---

- Treatment of initial conditions and parameters
  - How can we deal with all “possible worlds”?
- Comparing ABMs’ outputs and real-world observations
  - Simulated Distributions vs. Unique Real-World Observations
- **Unconditional Objects Critique**
  - If many processes are able to explain the same set of SFs, what does replication of SFs add to our knowledge?

# Hot Issues in Empirical Validation of ABMs

---

- Treatment of initial conditions and parameters
  - How can we deal with all “possible worlds”?
- Comparing ABMs’ outputs and real-world observations
  - Simulated Distributions vs. Unique Real-World Observations
- Unconditional Objects Critique
  - If many processes are able to explain the same set of SFs, what does replication of SFs add to our knowledge?
- **Is available data sufficient?**
  - Need for additional, more detailed microeconomics data
  - Need to validate microeconomic foundations with experimental data



# Ex 1: Qualitative Simulation Modeling

---

# Ex 1: Qualitative Simulation Modeling

---

- No empirical validation
  - Model as a laboratory to gain knowledge on the underlying causal relationships **only**, not taken to the data

# Ex 1: Qualitative Simulation Modeling

---

- No empirical validation
  - Model as a laboratory to gain knowledge on the underlying causal relationships **only**, not taken to the data
- Stylized Qualitative Models (Evolutionary-Games)
  - Weak relation between micro-macro variables/parameters in the model and empirically observed counterparts
  - Interest in explaining the emergence of qualitative aggregate pattern (cooperation, coordination, etc.)

# Ex 1: Qualitative Simulation Modeling

---

- No empirical validation
  - Model as a laboratory to gain knowledge on the underlying causal relationships **only**, not taken to the data
- Stylized Qualitative Models (Evolutionary-Games)
  - Weak relation between micro-macro variables/parameters in the model and empirically observed counterparts
  - Interest in explaining the emergence of qualitative aggregate pattern (cooperation, coordination, etc.)
- Early Evolutionary- and Industry-Dynamics Models
  - Much more micro-founded and empirically-driven, but...
  - If any, empirical validation is done in very weak ways

# Ex 1: Qualitative Simulation Modeling

---

- No empirical validation
  - Model as a laboratory to gain knowledge on the underlying causal relationships **only**, not taken to the data
- Stylized Qualitative Models (Evolutionary-Games)
  - Weak relation between micro-macro variables/parameters in the model and empirically observed counterparts
  - Interest in explaining the emergence of qualitative aggregate pattern (cooperation, coordination, etc.)
- Early Evolutionary- and Industry-Dynamics Models
  - Much more micro-founded and empirically-driven, but...
  - If any, empirical validation is done in very weak ways
- A pessimistic view about empirical validation?
  - Socio-economics: open-endedness, interdependence, structural change
  - Precise quantitative implications are difficult to obtain

# Ex 2: Replication of Stylized-Facts

---

# Ex 2: Replication of Stylized-Facts

---

- Indirect Calibration

- Detailed data able to restrict the set of initial conditions and micro/macro parameters is difficult to gather (Kaldor)
- Empirical validation is done at the aggregate (macroeconomic) level
- Parameters and initial conditions are not restricted a priori
- Validation requires joint reproduction of a set of “stylized facts” (SFs)

# Ex 2: Replication of Stylized-Facts

---

- Indirect Calibration

- Detailed data able to restrict the set of initial conditions and micro/macro parameters is difficult to gather (Kaldor)
- Empirical validation is done at the aggregate (macroeconomic) level
- Parameters and initial conditions are not restricted a priori
- Validation requires joint reproduction of a set of “stylized facts” (SFs)

- Four-Step Procedure (Fagiolo et al., 2004)

- **Step 1:** Identifying set of SFs of interest to be explained/reproduced
- **Step 2:** Keep microeconomics as close as possible to “real-world”
- **Step 3:** Find parameters and initial conditions for which the model is statistically able jointly to replicate the set of SFs
- **Step 4:** Investigation of subspace of parameters and initial conditions which “resist” to Step 3 in order to seek for causal relationships (explanations)



# Ex 3: Empirical Calibration of ABMs

---

# Ex 3: Empirical Calibration of ABMs

---

- Werker and Brenner (2005)
  - Dealing with space of initial conditions and micro/macro parameters
  - Difficult to employ theoretical arguments to restrict the set
  - Use empirical knowledge first to calibrate initial conditions and micro/macro parameters and then to validate

# Ex 3: Empirical Calibration of ABMs

---

- Werker and Brenner (2005)
  - Dealing with space of initial conditions and micro/macro parameters
  - Difficult to employ theoretical arguments to restrict the set
  - Use empirical knowledge first to calibrate initial conditions and micro/macro parameters and then to validate
- Three-Step Procedure
  - **Step 1:** Employ empirical knowledge to calibrate initial conditions and parameters ranges
  - **Step 2:** Further restricting initial conditions and parameters space by empirically validate simulated output with real-world data
  - **Step 3:** Abduction. Seek explanations of the phenomena under study by exploring properties of the “possible worlds” that resist to previous steps

# Ex 4: History-Friendly Industry Models

---

# Ex 4: History-Friendly Industry Models

---

- **Malerba, Nelson, Orsenigo, and co-authors**
  - Models built upon detailed empirical, anecdotic, historical knowledge of phenomenon under study and employed to replicate its precise (qualitative) history

# Ex 4: History-Friendly Industry Models

---

- Malerba, Nelson, Orsenigo, and co-authors
  - Models built upon detailed empirical, anecdotic, historical knowledge of phenomenon under study and employed to replicate its precise (qualitative) history
- Prominent role for empirical data
  - Detailed empirical (historical) data on the phenomenon under study assisting model building and validation
  - Specify agents' representation
  - Identify parameters and initial conditions
  - Empirically validate the model by comparing “simulated trace histories” with “actual history” of an industry

# Where do they differ?

---

# Where do they differ?

---

- Domain of application
  - Micro (industries, markets)
  - Macro (countries, world economy)



# Where do they differ?

---

- Domain of application
  - Micro (industries, markets)
  - Macro (countries, world economy)
- Which kind of empirical observations does one employ?
  - Empirical data about micro/macro variables
  - Casual, historical and anecdotic knowledge

# Where do they differ?

---

- Domain of application
  - Micro (industries, markets)
  - Macro (countries, world economy)
- Which kind of empirical observations does one employ?
  - Empirical data about micro/macro variables
  - Casual, historical and anecdotic knowledge
- How to employ empirical observations?
  - Assisting in model building (agents, behaviors, interactions,...)
  - Calibrating initial conditions and parameters
  - Validating simulated output

# Where do they differ?

---

- Domain of application
  - Micro (industries, markets)
  - Macro (countries, world economy)
- Which kind of empirical observations does one employ?
  - Empirical data about micro/macro variables
  - Casual, historical and anecdotic knowledge
- How to employ empirical observations?
  - Assisting in model building (agents, behaviors, interactions,...)
  - Calibrating initial conditions and parameters
  - Validating simulated output
- What to do first?
  - First calibrate, then validate
  - First validate, then calibrate
  - Validate only

## Input Validation via Iterative Participatory Modeling

---

- ◆ Joining together with industry stakeholders and researchers from multiple disciplines in a **repeated looping** through 4 stages of analysis:
  - Field work and data collection;
  - Scenario discussion/role-playing games;
  - Agent-based model development;
  - Intensive computational experiments.

**NOTE:** See Barreteau et al. (JASSS, 6-1,2003)

## Other Issues Related to the Empirical Validation of ACE Models

---

- How can researchers provide **summary reports** of model findings to other researchers and to intended model users (e.g. policy makers) in an accurate, compelling, and clear manner?

For example, it might be necessary to report **outcome distributions** rather than simple outcome point predictions.

Or it might be necessary to report how **network interaction patterns** vary systematically in response to policy changes.

# Other Issues...Continued

---

- How can researchers ensure the **robustness** of their model findings?

For example, how to be sure that model findings indeed arise from modeled attributes of a real-world system under study rather than from spurious aspects of the software/hardware platform implementation?

- How can researchers ensure the **accumulation** of empirically supported findings?