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The objectives of this paper are to:

- 1. formally define the weather premium in the U.S. corn market;
- 2. explore the factors that influence the weather premium; and
- 3. evaluate trading strategies that seek to exploit the weather premium.

Motivation

PARTICIPANTS IN the U.S. corn futures market often refer to a 'weather premium,' which refers to the tendency of the futures market to *over-predict* the actual harvest price.

If it exists, a weather premium rewards those who accept risk primarily associated with weather uncertainty. Market participants pay a premium to insure against adverse weather shocks.

Data from 1968 - 2015 suggests there may be a weather premium, as the December futures price in spring over estimates the realized harvest price by 4 percent.

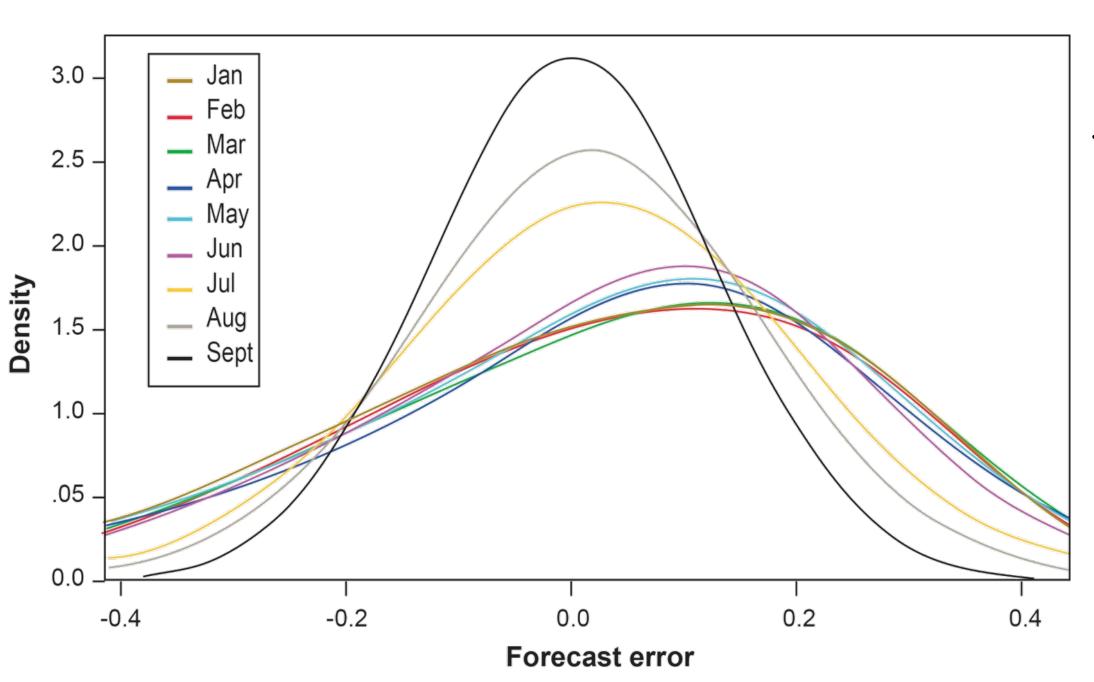


Figure 1. Density plots of the monthly average **December futures price of corn minus the harvest** price, expressed as a percentage of the harvest price, 1968-2015.

1. An increase in expected supply at harvest will have a negative impact on weather premium. 2. An increase in the variability of harvest quantity increases weather premium.

USING CHICAGO Mercantile Exchange corn futures data from 1968 - 2015, we analyze the *forecast errors* of the December futures contract by pooled OLS to test whether carryout, basis, and past yield provide explanatory power. A predictable component of the forecast errors is explained by variables capturing the distribution of the expected harvest.

• Forecast error in the December futures contract:

 $e_{t,j} \equiv \log(f_{t,j}) - \log(S_t)$, (Figure 3)

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The Weather Premium in the U.S. Corn Market

Theoretical Framework

SUPPOSE A CONVEX demand function $D(p_T)$ • p_T is the harvest price of corn in year T • $S_T = z_T + c_T$, supply at harvest • c_T : carryout available upon harvest • z_T : new production

$$z_T = \begin{cases} \bar{z} + \epsilon, \\ \bar{z} - \epsilon, \end{cases}$$

with probablity with probablity $\frac{1}{2}$

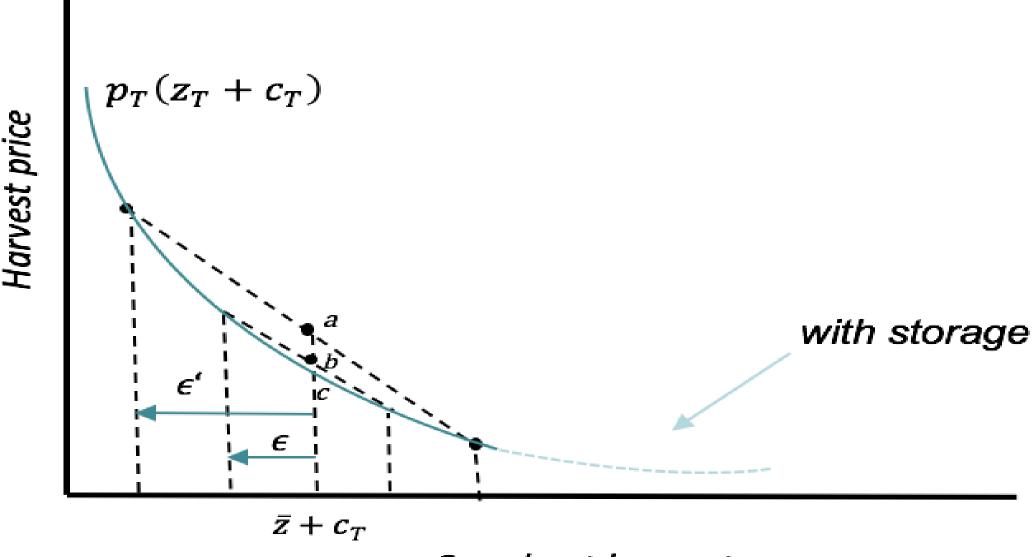
Definition: Weather premium is the expected harvest price minus the price given an average harvest: $E_t[p_T(S_T)] - p_T[E(S_T)]$

By Jensen's inequality: $E_t[p_T(S_T)]$ $p_T[E(S_T)] \ge 0$

WEATHER PREMIUM varies with the expectation and variation of supply at harvest. The comparative statics:

•
$$\begin{cases} \frac{1}{2} \left[\frac{\partial p_T}{\partial c_T} \middle|_{S_T = \bar{z} + c_T - \epsilon} + \frac{\partial p_T}{\partial c_T} \middle|_{S_T = \bar{z} - \epsilon} \right] \\ \frac{1}{2} \left[\frac{\partial p_T}{\partial \bar{z}} \middle|_{S_T = \bar{z} + c_T - \epsilon} + \frac{\partial p_T}{\partial \bar{z}} \middle|_{S_T = \bar{z} - \epsilon} \right] \end{cases}$$

•
$$-\frac{\partial p_T}{\partial \epsilon}|_{S_T = \bar{z} + c_T - \epsilon} + \frac{\partial p_T}{\partial \epsilon}|_{S_T = \bar{z} + c_T}$$



Supply at harvest

Data and Estimation Procedure

• $f_{t,j}$: monthly average prices of December futures in year t month j, j = January, ..., June

 \circ S_t: December futures price in the maturity month in year t

• Carryout is detrended by its 5-year average:

$$arry_t = \frac{c}{\sum_{i=t-1}^{i=t-1}}$$

 $carry_t$: marketing year's ending stock including harvest reported on August 31 in the USDA WASDE report.

- Temporal basis reflects cost of carry, and is the difference between the log futures prices for September and December delivery: $basis_{t,i} = \log(f_{t,Sept}) - \log(S_t)$
- Past Yield Measures Realizations

• Yield variability is normalize

$$vy_t = \sqrt{5 \sum_{i=t-5}^{t-1} (y_i - \sum_{i=t-5}^{t-1} y_i)}$$

• Detrended Yield level: dy_t :

Agricultural and Applied Economics Association Annual Meeting Chicago, Illinois July 31, 2017

$\bar{z} + c_T + \epsilon] - \frac{\partial p_T}{\partial c_T} |_{S_T = \bar{z} + c_T} \le 0$ $_{\bar{z}+c_{T}+\epsilon}] - \frac{\partial p_{T}}{\partial \bar{z}}|_{S_{T}=\bar{z}+c_{T}} \le 0$

 $c_{T+\epsilon} > 0.$

carry_t $\frac{1}{5} carry_i/n$

ed by its mean: $\sum_{i=t-5}^{\infty} y_{i}$

$$v_i / n)^2 / (\frac{\Delta l = l - 5 J l}{n})$$

$$= \log(y_t) - \log(\frac{\sum_{i=t-5}^{t-1} y_i}{n}).$$

Results

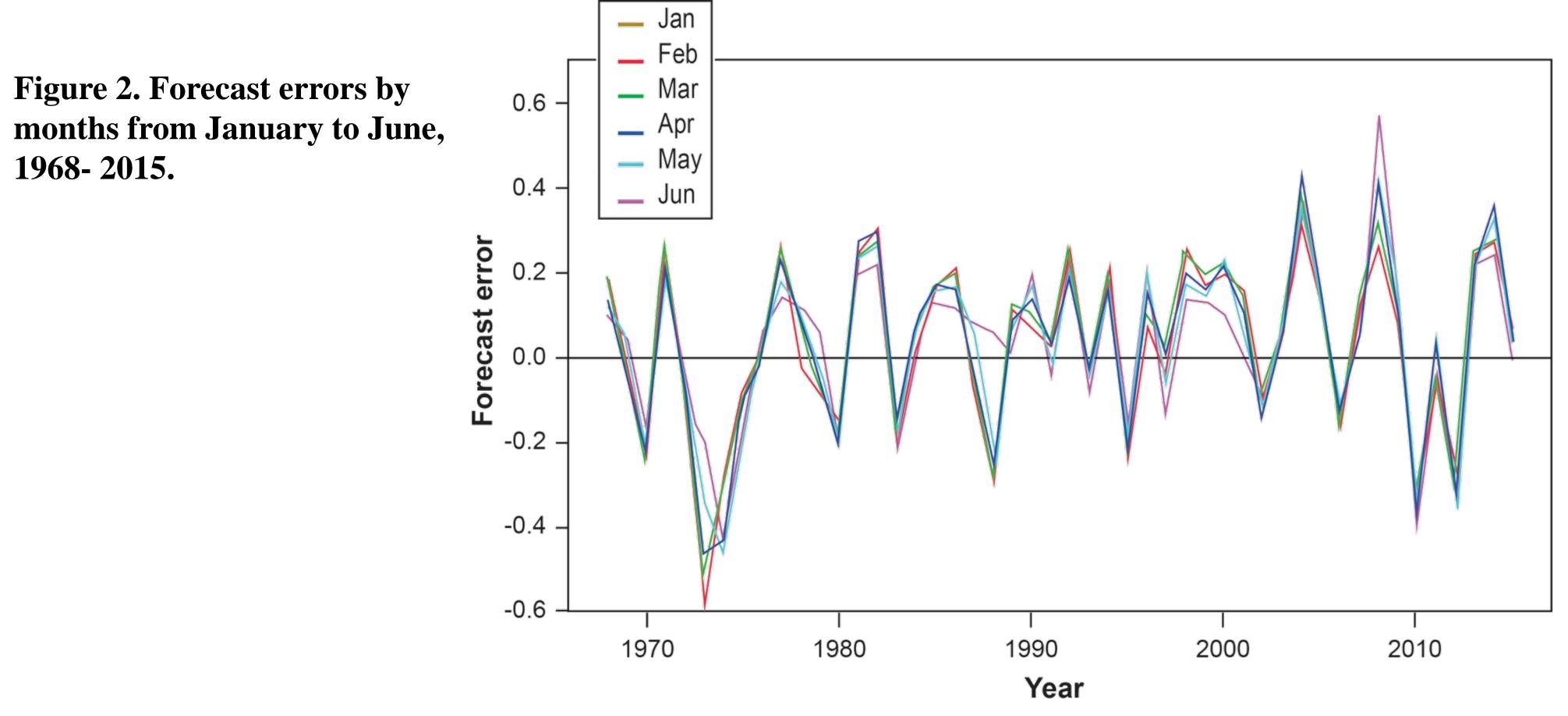
Empirical Model

Table 1. OLS Estimation of Corn Forecast Errors

	(1) Basis (Nearby futures – Dec. futures)	(2) Basis (Sep. futures – Dec. futures)	(3) Carryout	(4) Basis and carryout	(5) Full model	Strategies		Annualized Return	Standard Deviation	Sharpe Ratio
							Jan	0.014	0.279	0.049
const	0.078***	0.094***	0.510	1.059***	-0.595	Panel A: Short in spring and cover in October Panel B: Short in spring and cover in October, when carryout below trend	Feb	0.026	0.291	0.088
$carry_{t-1}^{2}$ $carry_{t-1}^{2}$	(0.022)	(0.022)	(0.657)	(0.665)	(0.854)		Mar			
			-0.436	-1.255	1.403			0.037	0.304	0.121
			(1.234)	(1.236)	(1.509)		Apr	0.043	0.327	0.133
			< 0.001	0.319	-0.663		May	0.044	0.339	0.131
vy_{t-1}			(0.576)	(0.572)	(0.674) 0.028		Jun	0.079	0.368	0.215
dy_{t-1}					(0.386)		Jan	0.142	0.168	0.847
					-0.858***		Feb	0.161	0.181	0.892
					(0.190)		Mar	0.180	0.206	0.874
$basis_{t,j} < 0$	-0.716**	-2.456***		-0.792	-1.274***		Apr	0.204	0.235	0.870
	(0.354)	(0.992)		(1.008)	(0.922)		May	0.212	0.275	0.772
$basis_{t,j} > 0$	0.241	1.405***		2.293***	2.695***		2			
	(0.245)	(0.637)		(0.641)	(0.625)		Jun	0.284	0.297	0.957
R^2	0.014	0.025	0.066	0.107	0.171		Buy in Jan and Cover in			
BP test for random	0.0890	0.0970	0.0870	0.0880	0.091		June, when	0.082	0.250	0.328
effects						Panel C: Other alternatives	carryout			
BP test for	0.273	0.666	< 0.001	< 0.001	< 0.001		above trend			
eteroscedasticity							S&P 500	0.078	0.165	0.476
Marginal impact of			-0.436***	-0.616*** (0.142)	0.077 (0.217)		Index	0.070	0.100	0.770

F-test

Note: Estimated robust standard errors are given in parentheses. Asterisks denote significance levels as follows: * indicates 10 percent; ** 5 percent; and *** 1 percent significance. Breusch-Pagan (BP) tests are performed for the presence of random effects and heteroscedasticity and the p-values are reported. The p-values of F-tests that compare model specification 4 to 3 and 5 to 4 are reported in columns 4 and 5, respectively.



$e_{t,j} = \beta_1 + \beta_2 carry_{t-1} + \beta_3 carry_{t-1}^2 + \beta_4 vy_{t-1} + \beta_5 dy_{t-1} + \gamma_1 basis_{t,j} \cdot 1_{\{basis_{t,j} < 0\}} + \gamma_2 basis_{t,j} \cdot 1_{\{basis_{t,j} > 0\}} + \rho_j + \xi_{t,j}$

Table 2. Returns of selected strategies.

14 of those years when carryout was below the average of the past 5 years. Panel C results are based on 34 of the years when carryout was above the average of the past 5 years. Data for the historical S&P 500 Index: https://finance.yahoo.com/quote/%5EGSPC/history?p=%5EGSPC