# A Bad Peace Is Better Than A Good War: 

A Structural Model of Marital Disagreements

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## Marital Disagreements in the U.S.

Typical disagreement frequencies (NSFH, married couples):

- once a week +: 39 percent
- several times a week $+: 23$ percent
- almost everyday: 11 percent

Common disagreement areas:

- household tasks, money, spending time together

Evidence on dispute resolution:

- seldom/never discuss disagreements: 27 percent
- often/always heatedly argue or shout: 10 percent


## Effects of Marital Disagreements

Impact on spouses (Booth et al., 2001):

- depression
- alcoholism, bad health
- poor parent-child relationship

Impact on children (Grych \& Fincham, 2001):

- low self-esteem, depression
- bad health
- conduct problems, trouble with law enforcement
- poor school performance
- low social competence

Amato et al. (1995), Jekielek (1998), Hanson (1999):

- conflict may be more detrimental to children than divorce


## Family Economics Literature

Marital dispute as outcome is absent in:

- unitary models (Becker, 1974)
- cooperative bargaining models (Manser \& Brown, 1980)
- collective models (Chiappori, 1988)

Separate spheres model (Lundberg \& Pollak, 1993):

- noncooperation is threat point, but cannot be outcome

Tartari (2005):

- presence of conflict is determined by exogenous stochastic process


## Novelty and Contribution

Novel features:

- three outcomes of bargaining: cooperation, open disagreement, divorce
- noncooperative framework (e.g., Friedberg \& Stern, 2006): allows for Pareto inferior outcomes
- two sources of asymmetric information
- adequate measure of "destructive" conflict
- detailed specification of divorce payoffs

Use the model to:

- quantify welfare losses due to marital conflict
- evaluate the effect of shorter separation periods
- analyze the impact of stronger child support enforcement


## Preview of Results

Effects on marital surplus:

- positive impact: husband's education level, age, catholic religion
- negative impact: differences in spousal ages and education levels

Effects on divorce options:

- positive impact: favorable marriage market conditions
- negative impact: separation period requirements

Most spouses are "soft bargainer - pessimists"

## Outline

- Model
- Data and Variables
- Econometric Specification
- Estimation Strategy
- Results
- Conclusion


## Bargaining Game Structure



## Bargaining Game Structure



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## Spousal Types and Husband's Beliefs

Two sources of unobserved heterogeneity:

- Bargaining "strength": "soft" $(S)$ vs. "hard" $(H)$ bargainer
- Divorce prospect: "pessimist" $(P)$ vs. "optimist" $(O)$

Spousal type ( $k$ ) combines trait levels:

- e.g., type $H O$ stands for "hard bargainer - optimist"
- $k \in\{H O, H P, S O, S P\}$

Knowledge about types:

- type is private information
- husband has beliefs $\left(\delta^{H O}, \delta^{H P}, \delta^{S O}, \delta^{S P}\right)^{\prime}$


## Utilities

Cooperation: utilities are type invariant:

- $u_{h}(-\tau)$ and $u_{w}(\tau)$

Open disagreement: bargaining "strength" matters:

- $v_{h}^{k}=\left\{\begin{array}{l}v_{h}^{H}, k=H O, H P \\ v_{h}^{S}, k=S O, S P\end{array}\right.$ and $v_{w}^{k}=\left\{\begin{array}{l}v_{w}^{H}, k=H O, H P \\ v_{w}^{S}, k=S O, S P\end{array}\right.$
- $v_{h}^{H}>v_{h}^{S}$ and $v_{w}^{H}>v_{w}^{S}$

Divorce: optimism matters:

- $y_{h}^{k}=\left\{\begin{array}{l}y_{h}^{O}, k=H O, S O \\ y_{h}^{P}, k=H P, S P\end{array}\right.$ and $y_{w}^{k}=\left\{\begin{array}{l}y_{w}^{O}, k=H O, S O \\ y_{w}^{P}, k=H P, S P\end{array}\right.$
- $y_{h}^{O}>y_{h}^{P}$ and $y_{w}^{O}>y_{w}^{P}$


## Solution Approach

Backward recursion:
stage 2: wife maximizes her utility
stage 1: husband anticipates wife's best response, maximizes his expected utility

Husband's strategies and expected utilities:

- strategies: $(\tau ; \mathcal{C}), \mathcal{R}, \mathcal{D}$
- expected utilities: $\hat{E} \mathcal{V}_{h}^{k}(\tau ; \mathcal{C}), \hat{E} \mathcal{V}_{h}^{k}(\mathcal{R}), \hat{E} \mathcal{V}_{h}^{k}(\mathcal{D})$

Technical issues:

- uncountably many transfers: game is infinite
- $\hat{E} \mathcal{V}_{h}^{k}(\tau ; \mathcal{C})$ is discontinuous in $\tau$


## Game Properties

## Theorem

All strategies $(\tau ; \mathcal{C})$ with $\tau: u_{h}(-\tau)<y_{h}^{k}$ are dominated.

## Theorem

Strategy $\mathcal{R}$ is dominated.

## Theorem

Let $T^{k}=\left\{\tau: u_{h}(-\tau) \geq y_{h}^{k}\right\}$. Solution to husband's problem:

$$
\max _{\{\mathcal{C}, \mathcal{D}\}}\left\{\max _{\tau \in T^{k}} \hat{E} \mathcal{V}_{h}^{k}(\tau ; \mathcal{C}), \hat{E} \mathcal{V}_{h}^{k}(\mathcal{D})\right\}
$$

always exists.

## Simplified Game Structure



## Simplified Game Structure



## Simplified Game Structure



## Primary Data Source: NSFH

National Survey of Families and Households (NSFH):

- nationally representative panel of households
- 3 data collection waves: 1987-88, 1992-94, 2001-02
- variety of information on family life
- spouses answered separate questionnaires
- initial sample: 5,270 married couples

Analyzed sample:

- 3,878 married couples
- reasons for exclusion from initial sample:
- missing data (575 couples)
- attrition (477 couples)
- spousal death (340 couples)


## Additional Data Sources

Marriage market conditions:

- availability ratio (Goldman et al., 1984)
- source: 1990 Census (5-percent PUMS)

Divorce regulations:

- separation period requirements
- source: Friedberg (1998)

Child support enforcement:

- collection rate (Nixon, 1997)
- source: Office of CSE reports to Congress


## Marital and Spousal Characteristics

| Variable | Mean | (Std.Dev.) | Min | Max |
| :--- | ---: | ---: | ---: | ---: |
| children, $<6$ year old | 0.45 | $(0.73)$ | 0 | 5 |
| children, $\geq 6$ year old | 0.57 | $(0.94)$ | 0 | 5 |
| children, wife's | 0.14 | $(0.47)$ | 0 | 5 |
| marriage duration | 14.51 | $(13.23)$ | 0 | 63.58 |
| home ownership | 0.75 | $(0.43)$ | 0 | 1 |
| age, husband's | 41.02 | $(13.75)$ | 17 | 90 |
| age, absolute difference | 3.62 | $(3.84)$ | 0 | 38 |
| black husband | 0.09 | $(0.29)$ | 0 | 1 |
| catholic husband | 0.23 | $(0.42)$ | 0 | 1 |
| religion, difference | 0.33 | $(0.47)$ | 0 | 1 |
| high school, husband | 0.51 | $(0.50)$ | 0 | 1 |
| college, husband | 0.33 | $(0.47)$ | 0 | 1 |
| education, difference | 0.38 | $(0.48)$ | 0 | 1 |

## Location-Specific Data, Beliefs, and Opinions

| Variable | Mean | (Std.Dev.) | Min | Max |
| :--- | ---: | ---: | ---: | ---: |
| availability ratio, husband | 1.25 | $(0.24)$ | 0.56 | 2.43 |
| availability ratio, wife | 0.84 | $(0.16)$ | 0.22 | 1.45 |
| separation, $\leq 1$ year | 0.18 | $(0.39)$ | 0 | 1 |
| separation, $>1$ year | 0.33 | $(0.47)$ | 0 | 1 |
| collection rate | 0.11 | $(0.10)$ | 0 | 0.35 |
| same happiness, belief | 0.19 | $(0.39)$ | 0 | 1 |
| more happy, belief | 0.08 | $(0.27)$ | 0 | 1 |
| same happiness, husband | 0.17 | $(0.38)$ | 0 | 1 |
| more happy, husband | 0.06 | $(0.23)$ | 0 | 1 |
| worthy person, husband | 0.38 | $(0.49)$ | 0 | 1 |
| same happiness, wife | 0.15 | $(0.36)$ | 0 | 1 |
| more happy, wife | 0.07 | $(0.26)$ | 0 | 1 |
| worthy person, wife | 0.42 | $(0.49)$ | 0 | 1 |

## Marital State

## Divorce:

- legally divorced or separated as of wave 2

Open disagreement:

- disagree about at least one aspect of marriage as of wave 2
- disputes occur several times a week or more often
- seldom/never discuss disputes or often/always shout

Cooperation:

- intact couples not in the state of open disagreement

| Marital State | Frequency | Share (\%) |
| :--- | ---: | ---: |
| cooperation | 2,948 | 76.02 |
| open disagreement | 416 | 10.73 |
| divorce | 514 | 13.25 |
|  | Total | 3,878 |

## Parameterized Utilities

## Husband

Cooperation:

$$
u_{h}=x^{\prime} \alpha_{h}-\tau+\theta_{1}
$$

$$
u_{w}=x^{\prime} \alpha_{w}+\tau+\theta_{3}
$$

Disagreement:

$$
v_{h}^{S}=x^{\prime} \beta_{h}+\theta_{2}
$$

$$
v_{w}^{S}=x^{\prime} \beta_{w}+\theta_{4}
$$

$$
v_{h}^{H}=v_{h}^{S}+\beta_{h}^{H}
$$

$$
v_{w}^{H}=v_{w}^{S}+\beta_{w}^{H}
$$

Divorce:

$$
\begin{aligned}
& y_{h}^{P}=z_{h}^{\prime} \gamma_{h} \\
& y_{h}^{O}=y_{h}^{P}+\gamma_{h}^{O}
\end{aligned}
$$

$$
y_{w}^{P}=z_{w}^{\prime} \gamma_{w}
$$

$$
y_{w}^{O}=y_{w}^{P}+\gamma_{w}^{O}
$$

- $x$ : vector of marital and spousal data
- list of variables
- $z_{h}, z_{w}$ : vectors of location-specific data
- lists of variables
- type-specific constants: $\beta_{h}^{H}, \beta_{w}^{H}, \gamma_{h}^{O}, \gamma_{w}^{O}>0$
- cannot separately identify $\alpha_{h}$ and $\alpha_{w}$; estimate $\alpha \equiv \alpha_{h}+\alpha_{w}$


## Parameterized Type Probabilities and Beliefs

Type probabilities (Degan \& Merlo, 2006):

$$
\pi_{h}^{k}=\frac{\exp \left(a_{h}^{\prime} \lambda_{h}^{k}\right)}{\sum_{j} \exp \left(a_{h}^{\prime} \lambda_{h}^{j}\right)}, \pi_{w}^{k}=\frac{\exp \left(a_{w}^{\prime} \lambda_{w}^{k}\right)}{\sum_{j} \exp \left(a_{w}^{\prime} \lambda_{w}^{j}\right)}
$$

- $a_{h}, a_{w}$ : vectors of spousal answers lists of varibles
- normalization: $\lambda_{h}^{S P}=0$ and $\lambda_{w}^{S P}=0$

Husband's beliefs:

$$
\delta^{k}=\frac{\exp \left(b^{\prime} \rho^{k}+\eta^{k}\right)}{\sum_{j} \exp \left(b^{\prime} \rho^{j}+\eta^{j}\right)}
$$

- $b$ : vector of husband's reported beliefs
- normalization: $\rho^{S P}=0$ and $\eta^{S P}=0$


## Distributions of Unobservables

Unobservable components of utilities:

$$
\underset{4 \times 1}{\theta} \sim \text { i.i.d. } N(0, \Sigma)
$$

Unobservable components of beliefs:

$$
\underset{3 \times 1}{\eta} \sim \text { i.i.d. } N(0, \Omega)
$$

## Overview of Estimation Approach

Strategy:

- use data as of wave 1 to predict marital state as of wave 2
- express marital state probabilities in easy to simulate way
- find parameters by maximum simulated likelihood method

Implementation:

- solve for marital state probabilities in terms of conditional probabilities given spousal types
- express conditional probability as integral of indicator function
- find boundaries of integration analytically
- simulate integrals by GHK


## Estimation Specifics

## Notation:

- marital state: $s$
- data: $X$ list of variables
- parameters: $\Gamma \backsim$ list of parameters

Marital state probability:

$$
\operatorname{Pr}[s=\operatorname{coop} . \mid X, \Gamma]=\sum_{k} \sum_{l} \pi_{h}^{k} \cdot \pi_{w}^{l} \cdot \operatorname{Pr}[s=\operatorname{coop} . \mid k, l, X, \Gamma]
$$

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$$

Conditional marital state probability:

$$
\operatorname{Pr}[s=\text { coop. } \mid k, l, X, \Gamma]=E_{\theta, \eta} \mathbf{1}\left(\begin{array}{l}
\tau^{*}=\arg \max _{\tau} \hat{E} \mathcal{V}_{h}^{k}(\tau ; \mathcal{C}), \\
\hat{E} \mathcal{V}_{h}^{k}\left(\tau^{*} ; \mathcal{C}\right) \geq y_{h}^{k} \\
u_{w}\left(\tau^{*}\right) \geq v_{w}^{l} \\
u_{w}\left(\tau^{*}\right) \geq y_{w}^{l}
\end{array}\right)
$$

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u_{w}\left(\tau^{*}\right) \geq v_{w w}^{l} \\
u_{w}\left(\tau^{*}\right) \geq y_{w}^{l}
\end{array}\right)
$$

## Integration Bounds

Simulation approach:

- transform $E_{\theta, \eta} \mathbf{1}(\theta, \eta \in S)=\int_{S} f(\theta, \eta) d \theta d \eta$ : solve for integration bounds that represent set $S$
- simulate $\int_{S} f(\theta, \eta) d \theta d \eta$ with GHK

Transformation algorithm:
step 1: partition $\theta_{4}$ domain; then, on each interval:
step 2: find discontinuity points of $\hat{E} \mathcal{V}_{h}^{k}(\tau ; \mathcal{C})$
step 3: find acceptable transfer(s) to wife of type $l$
step 4: write out inequalities when husband of type $k$ chooses to offer such transfer(s)
step 5: solve inequalities for integration bounds example
step 6: repeat steps $2-5$ for all $\theta_{4}$ intervals

## Intact Marriage Utilities

Cooperation
$\left.\begin{array}{lcccccc}\text { Variable } & \text { Coeff. } & \text { Std.Err. } & \text { Coeff. } & \text { Std.Err. } & \text { Coeff. } & \text { Std.Err. } \\ \hline \text { constant } & 4.4799^{* * *} & (0.0890) & -3.3420^{* * *} & (0.0945) & -0.4905^{* * *} & (0.0726) \\ \text { children, }<6 \text { y.o. } & 0.2367^{* * *} & (0.0690) & -0.3217^{* * *} & (0.0760) & 0.2362^{* * *} & (0.0686) \\ \text { children, } \geq 6 \text { y.o. } & 0.0208 & (0.0634) & 0.4793^{* * *} & (0.0607) & 0.5113^{* * *} & (0.0521) \\ \text { children, wife's } & -0.1823^{* * *} & (0.0673) & 0.2131^{* * *} & (0.0798) & 0.5708^{* * *} & (0.0733) \\ \text { duration } & 1.1308^{* * *} & (0.0789) & 0.1018 & (0.0830) & -0.3311^{* * *} & (0.0583) \\ \text { home ownership } & 0.0988 & (0.0857) & 1.1574^{* * *} & (0.0859) & -0.1530^{* *} & (0.0716) \\ \text { age, husb.'s } & 0.5055^{* * *} & (0.0712) & 1.7136^{* * *} & (0.0722) & 0.0839 & (0.0597) \\ \text { age, abs. diff. } & -0.1430^{* * *} & (0.0530) & -0.7814^{* * *} & (0.0699) & -0.0080 & (0.0502) \\ \text { black husb. } & 0.3063^{* * *} & (0.0818) & -1.4418^{* * *} & (0.0798) & 0.4589^{* * *} & (0.0930) \\ \text { catholic husb. } & 0.2397^{* * *} & (0.0858) & 0.8132^{* * *} & (0.0948) & 0.2994^{* * *} & (0.0726) \\ \text { religion, diff. } & 0.0551 & (0.0728) & -0.8312^{* * *} & (0.0836) & 0.0080 & (0.0684) \\ \text { high sch., husb. } & 0.3271^{* * *} & (0.0688) & 0.8873^{* * *} & (0.0853) & -0.3419^{* * *} & (0.0723) \\ \text { college, husb. } & 0.2457^{* * *} & (0.0808) & 0.1665^{* *} & (0.0763) & -0.9109^{* * *} & (0.0659) \\ \text { education, diff. } & -0.2787^{* * *} & (0.0763) & 0.1530^{*} & (0.0796) & 0.3574^{* * *} & (0.0680) \\ \text { HO/HP constant } & & - & & 3.1811^{* * *} & (0.1497) & 2.7123^{* * *}\end{array}\right)(0.1125)$
*, **, and ${ }^{* * *}$ denote significance at 10,5 , and 1 percent levels.

## Divorce Utilities

|  | Husband |  | Wife |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Variable | Coeff. | Std.Err. | Coeff. | Std.Err. |  |
| availability ratio, husband | $0.4030^{* * *}$ | $(0.0613)$ | - |  |  |
| availability ratio, wife | - |  |  | $1.5427^{* * *}$ | $(0.0810)$ |
| separation, $\leq 1$ year | $-0.1464^{*}$ | $(0.0792)$ | -0.0002 | $(0.0753)$ |  |
| separation, $>1$ year | $-0.2091^{* * *}$ | $(0.0770)$ | $-0.3166^{* * *}$ | $(0.0772)$ |  |
| collection rate | $-0.4174^{* * *}$ | $(0.0922)$ | 0.0001 | $(0.0929)$ |  |
| HO/SO constant | $3.6410^{* * *}$ | $(0.1763)$ | $0.5688^{* * *}$ | $(0.0374)$ |  |

${ }^{*},{ }^{* *}$, and ${ }^{* * *}$ denote significance at 10,5 , and 1 percent levels.

## Type Probabilities and Beliefs

|  | True Types |  | Beliefs |  |
| :--- | :--- | ---: | ---: | ---: |
| Spousal Type | Husband | Wife | Husband |  |
| HO | (hard bargainer - optimist) | 0.1086 | 0.0382 | 0.0943 |
| HP | (hard bargainer - pessimist) | 0.1264 | 0.2420 | 0.0466 |
| SO | (soft bargainer - optimist) | 0.0146 | 0.0516 | 0.1165 |
| SP | (soft bargainer - pessimist) | 0.7505 | 0.6682 | 0.7426 |

## Conclusion

Key contributions:

- marital dispute is outcome of bargaining
- model allows for Pareto inferior outcome and information asymmetry
- disagreement indicator incorporates data on conflict resolution
- policy variables affect divorce payoffs

Further directions:

- evaluation of welfare effects
- analysis of policy changes


## Questions?

## Appendix Outline

- Appendix
- Husband's Expected Utilities
- Explanatory Vectors
- Vectors of Answers and Beliefs
- Data Vector
- Parameter Vector
- Integration Bounds Example
- Integration Bounds Example (Continued)
- Intact Marriage Utilities (w/o P.E. Variables)
- Divorce Utilities (w/o P.E. Variables)
- Type Probabilities and Beliefs (w/o P.E. Variables)
- Reduced Form Trinomial Model
- Reduced Form Trinomial Model (w/o P.E. Variables)


## Husband's Expected Utilities

Action $(\tau ; \mathcal{C})$ :

$$
\begin{aligned}
& \hat{E} \mathcal{V}_{h}^{k}(\tau ; \mathcal{C})=\sum_{l} \delta^{l}\left[y_{h}^{k} \cdot \mathbf{1}\binom{y_{w}^{l}>v_{w}^{l}}{y_{w}^{l}>u_{w}(\tau)}+\right. \\
&+v_{h}^{k} \cdot \mathbf{1}\binom{v_{w}^{l} \geq y_{w}^{l}}{v_{w}^{l}>u_{w}(\tau)}+ \\
&\left.+u_{h}(-\tau) \cdot \mathbf{1}\binom{u_{w}(\tau) \geq y_{w}^{l}}{u_{w}(\tau) \geq v_{w}^{l}}\right] .
\end{aligned}
$$

Action $\mathcal{R}$ :

$$
\hat{E} \mathcal{V}_{h}^{k}(\mathcal{R})=\sum_{l} \delta^{l}\left[y_{h}^{k} \cdot \mathbf{1}\left(y_{w}^{l}>v_{w}^{l}\right)+v_{h}^{k} \cdot \mathbf{1}\left(v_{w}^{l} \geq y_{w}^{l}\right)\right]
$$

Action $\mathcal{D}$ :

$$
\hat{E} \mathcal{V}_{h}^{k}(\mathcal{D})=y_{h}^{k}
$$

## Explanatory Vectors

| $x$ | $z_{h}$ | $z_{w}$ |
| :--- | :--- | :--- |
| constant | avail. ratio, husb. | avail. ratio, wife |
| children, $<6$ y.o. | separation, $\leq 1$ year | separation, $\leq 1$ year |
| children, $\geq 6$ y.o. | separation, $>1$ year | separation, $>1$ year |
| children, wife's | collection rate | collection rate |
| duration (std) |  |  |
| home ownership |  |  |
| age, husb.'s (std) |  |  |
| age, abs. diff. (std) |  |  |
| black husb. |  |  |
| catholic husb. |  |  |
| religion, diff. |  |  |
| high sch., husb. |  |  |
| college, husb. |  |  |
| education, diff. |  |  |

## Vectors of Answers and Beliefs

| $a_{h}$ | $a_{w}$ | $b$ |
| :--- | :--- | :--- |
| constant | constant | constant |
| same happiness, husb. | same happiness, wife | same happiness |
| more happy, husb. | more happy, wife | more happy |
| worthy person, husb. | worthy person, wife |  |
|  | \& back to parameterized types and beliefs |  |

## Data Vector

$x$ marital and spousal characteristics
$z_{h}$ location-specific characteristics of husband
$z_{w}$ location-specific characteristics of wife
$a_{h}$ husband's own divorce prospect and opinions
$a_{w} \quad$ wife's own divorce prospect and opinions
$b$ husband's beliefs about wife's divorce prospect
4 back to estimation specifics

## Parameter Vector

$\alpha \quad$ parameters of $u_{h}+u_{w}$
$\beta_{h} \quad$ parameters of $v_{h}^{S}$ and $v_{h}^{H}$
$\beta_{h}^{H} \quad$ hard bargainer's constant for husband, $\beta_{h}^{H}>0$
$\beta_{w} \quad$ parameters of $v_{w}^{S}$ and $v_{w}^{H}$
$\beta_{w}^{H} \quad$ hard bargainer's constant for wife, $\beta_{w}^{H}>0$
$\gamma_{h}$ parameters of $y_{h}^{P}$ and $y_{h}^{O}$
$\gamma_{h}^{O}$ optimist's constant for husband, $\gamma_{h}^{O}>0$
$\gamma_{w} \quad$ parameters of $y_{w}^{P}$ and $y_{w}^{O}$
$\gamma_{w}^{O}$ optimist's constant for wife, $\gamma_{w}^{O}>0$
$\lambda_{h}^{k} \quad$ parameters of $\pi_{h}^{k}, k=\{H O, H P, S O, S P\}$
$\lambda_{w}^{k} \quad$ parameters of $\pi_{w}^{k}, k=\{H O, H P, S O, S P\}$
$\rho^{k} \quad$ parameters of $\delta^{k}, k=\{H O, H P, S O, S P\}$
$\Sigma$ covariance matrix of $\theta$
$\Omega \quad$ covariance matrix of $\eta$

## Integration Bounds Example

The example shows a small part of the integration region for the state of cooperation when husband's type is $k$ (generic) and wife's type is $S P(l=S P)$ :

$$
I_{5}^{C}=\int_{\Re^{3}} \int_{f_{1}}^{f_{2}} \int_{-\infty}^{+\infty} \int_{f_{3}\left(\eta, \theta_{4}\right)}^{+\infty} \int_{f_{4}\left(\eta, \theta_{2}, \theta_{3}\right)}^{f_{5}\left(\eta, \theta_{2}, \theta_{3}, \theta_{4}\right)} f(\theta, \eta) d \theta_{1} d \theta_{2} d \theta_{3} d \theta_{4} d \eta
$$

Definitions:

$$
\begin{aligned}
f_{1} & =y_{w}^{P}-\bar{v}_{w}^{H} \\
f_{2} & =\min \left\{y_{w}^{P}-\bar{v}_{w}^{S}, y_{w}^{O}-\bar{v}_{w}^{H}\right\} \\
f_{3}\left(\eta, \theta_{4}\right) & =y_{h}^{k}-\bar{v}_{h}^{k}+\frac{\delta^{S P}(\eta)}{\delta^{H P}(\eta)}\left(y_{w}^{P}-\bar{v}_{w}^{H}\right)-\frac{\delta^{S P}(\eta)}{\delta^{H P}(\eta)} \theta_{4}
\end{aligned}
$$

## Integration Bounds Example (Continued)

Definitions (continued):

$$
\begin{aligned}
f_{4}\left(\eta, \theta_{2}, \theta_{3}\right)= & -\bar{u}_{h}-\bar{u}_{w}-\theta_{3}+ \\
& +\max \left\{\begin{array}{c}
y_{h}^{k}+y_{w}^{P}, \\
y_{w}^{P}+\frac{\left(\delta^{H P}(\eta)+\delta^{S P}(\eta)\right) y_{h}^{k}-\delta^{H P}(\eta)\left(\bar{v}_{h}^{k}+\theta_{2}\right)}{\delta^{S P}(\eta)}
\end{array}\right\}
\end{aligned}
$$

$$
\begin{aligned}
& f_{5}\left(\eta, \theta_{2}, \theta_{3}, \theta_{4}\right)=-\bar{u}_{h}-\bar{u}_{w}-\theta_{3}+ \\
& \quad+\min \left\{\begin{array}{l}
\bar{v}_{h}^{k}+\theta_{2}+\frac{\left(\delta^{H P}(\eta)+\delta^{S P}(\eta)\right)\left(\bar{z}_{w}^{H}+\theta_{4}\right)-\delta^{S P}(\eta) y_{w}^{P}}{\delta^{H P}}, \\
\frac{\left(\delta^{H O}(\eta)+\delta^{S O}(\eta)\right) y_{h}^{k}+\delta^{H P}(\eta)\left(\bar{v}_{h}^{k}+\theta_{2}\right)+y_{w}^{O}-\delta^{S P}(\eta) y_{w}^{P}}{1-\delta^{S P}(\eta)}
\end{array}\right\}
\end{aligned}
$$

## Intact Marriage Utilities (w/o P.E. Variables)

## Cooperation

| Variable | Coeff. | Std.Err. | Coeff. | Std.Err. | Coeff. | Std.Err. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| constant | 3.4776*** | (0.0604) | $-3.2457^{* * *}$ | (0.0674) | -0.4973*** | (0.0697) |
| children, $<6$ y.o. |  |  |  |  |  |  |
| children, $\geq 6$ y.o. |  |  | - |  | - |  |
| children, wife's | $-0.2237^{* * *}$ | (0.0468) | 0.0726 | (0.0736) | $0.1554^{* * *}$ | (0.0578) |
| duration |  |  | - |  |  |  |
| home ownership | - |  | - |  | - |  |
| age, husb.'s | 0.7119*** | (0.0465) | 1.2218*** | (0.0615) | $-0.3976 * * *$ | (0.0452) |
| age, abs. diff. | $-0.2985^{* * *}$ | (0.0320) | $-0.2235^{* * *}$ | (0.0514) | $0.1895^{* * *}$ | (0.0395) |
| black husb. | -0.0532 | (0.0629) | $-0.8016^{* * *}$ | (0.0736) | $0.3347^{* * *}$ | (0.0616) |
| catholic husb. | 0.2120*** | (0.0501) | $0.2921^{* * *}$ | (0.0668) | $0.1697^{* * *}$ | (0.0642) |
| religion, diff. | $-0.1561^{* * *}$ | (0.0560) | -0.0645 | (0.0666) | 0.1055 | (0.0679) |
| high sch., husb. | $0.1586{ }^{* * *}$ | (0.0584) | $0.3507^{* * *}$ | (0.0723) | $-0.3929^{* * *}$ | (0.0609) |
| college, husb. | $0.3386^{* * *}$ | (0.0582) | $-0.2169^{* * *}$ | (0.0769) | $-0.9688^{* * *}$ | (0.0634) |
| education, diff. | $-0.3138^{* * *}$ | (0.0528) | $0.5966^{* * *}$ | (0.0715) | $0.3030^{* * *}$ | (0.0626) |
| HO/HP constant | - |  | $3.5164^{* * *}$ | (0.1186) | $2.9047^{* * *}$ | (0.1012) |

*, **, and ${ }^{* * *}$ denote significance at 10,5 , and 1 percent levels.

## Divorce Utilities (w/o P.E. Variables)

|  | Husband |  | Wife |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Variable | Coeff. | Std.Err. | Coeff. | Std.Err. |  |
| availability ratio, husband | $0.2274^{* * *}$ | $(0.0555)$ | - |  |  |
| availability ratio, wife | - |  |  | $1.5431^{* * *}$ | $(0.0560)$ |
| separation, $\leq 1$ year | -0.0584 | $(0.0597)$ | -0.0002 | $(0.0610)$ |  |
| separation, $>1$ year | -0.0768 | $(0.0570)$ | $-0.2196^{* * *}$ | $(0.0595)$ |  |
| collection rate | $-0.3066^{* * *}$ | $(0.0795)$ | 0.0001 | $(0.0634)$ |  |
| HO/SO constant | $2.4080^{* * *}$ | $(0.1040)$ | $0.3087^{* * *}$ | $(0.0161)$ |  |

${ }^{*},{ }^{* *}$, and ${ }^{* * *}$ denote significance at 10,5 , and 1 percent levels.

## Type Probabilities and Beliefs (w/o P.E. Variables)

|  | True Types |  | Beliefs |  |
| :--- | :--- | ---: | ---: | ---: |
| Spousal Type | Husband | Wife | Husband |  |
| HO | (hard bargainer - optimist) | 0.0977 | 0.0428 | 0.0735 |
| HP | (hard bargainer - pessimist) | 0.1336 | 0.2449 | 0.0536 |
| SO | (soft bargainer - optimist) | 0.0119 | 0.0373 | 0.0874 |
| SP | (soft bargainer - pessimist) | 0.7568 | 0.6750 | 0.7856 |

## Reduced Form Trinomial Model

|  | Open Disagreement |  | Divorce |  |
| :--- | :---: | :---: | :---: | :---: |
| Variable | Coeff. | Std.Err. | Coeff. | Std.Err. |
| constant | $-2.1053^{* * *}$ | $(0.5154)$ | $-2.3055^{* * *}$ | $(0.5307)$ |
| children, $<6$ y.o. | 0.0341 | $(0.0612)$ | -0.0627 | $(0.0604)$ |
| children, $\geq 6$ y.o. | $0.1251^{* * *}$ | $(0.0479)$ | $0.0962^{*}$ | $(0.0515)$ |
| children, wife's | $0.1426^{*}$ | $(0.0825)$ | $0.1594^{* *}$ | $(0.0766)$ |
| duration | -0.0776 | $(0.0858)$ | $-0.4670^{* * *}$ | $(0.0931)$ |
| home ownership | $-0.2451^{* * *}$ | $(0.0892)$ | $-0.3002^{* * *}$ | $(0.0847)$ |
| age, husb.'s | $-0.3631^{* * *}$ | $(0.1017)$ | $-0.3904^{* * *}$ | $(0.0969)$ |
| age, abs. diff. | $0.1182^{* * *}$ | $(0.0453)$ | $0.1928^{* * *}$ | $(0.0439)$ |
| black husb. | $0.3901^{* * *}$ | $(0.1340)$ | $0.4010^{* * *}$ | $(0.1394)$ |
| catholic husb. | $0.1703^{*}$ | $(0.0894)$ | -0.1259 | $(0.0930)$ |
| religion, diff. | 0.1303 | $(0.0823)$ | $0.1619^{* *}$ | $(0.0796)$ |
| high sch., husb. | $-0.3716^{* * *}$ | $(0.1171)$ | $-0.2770^{* *}$ | $(0.1224)$ |
| college, husb. | $-0.4728^{* * *}$ | $(0.1220)$ | $-0.5409^{* * *}$ | $(0.1244)$ |
| education, diff. | $0.1336^{*}$ | $(0.0809)$ | $0.1798^{* *}$ | $(0.0807)$ |
| avail. ratio, husb. | $0.8260^{* * *}$ | $(0.2764)$ | $0.4914^{*}$ | $(0.2983)$ |
| avail. ratio, wife | -0.3923 | $(0.3654)$ | 0.5411 | $(0.3546)$ |
| separation, $\leq 1$ year | $-0.1874^{*}$ | $(0.1093)$ | -0.1096 | $(0.1046)$ |
| separation, $>1$ year | 0.0163 | $(0.0853)$ | $-0.2157^{* *}$ | $(0.0869)$ |
| collection rate | 0.7281 | $(0.5151)$ | 0.2811 | $(0.4985)$ |

${ }^{*},{ }^{* *}$, and ${ }^{* * *}$ denote significance at 10,5 , and 1 percent levels.

## Reduced Form Trinomial Model (w/o P.E. Variables)

| Variable | Open Disagreement |  | Divorce |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Coeff. | Std.Err. | Coeff. | Std.Err. |
| constant | $-2.0584^{* * *}$ | (0.4985) | -2.5020*** | (0.5095) |
| children, $<6$ y.o. | - |  |  |  |
| children, $\geq 6$ y.o. | - |  |  |  |
| children, wife's | 0.1115 | (0.0772) | $0.2398^{* *}$ | (0.0709) |
| duration |  |  |  |  |
| home ownership | - |  |  |  |
| age, husb.'s | $-0.4566{ }^{* * *}$ | (0.0700) | $-0.7374^{* * *}$ | (0.0715) |
| age, abs. diff. | $0.1417^{* * *}$ | (0.0394) | 0.2958*** | (0.0388) |
| black husb. | $0.4361^{* * *}$ | (0.1324) | $0.4363^{* * *}$ | (0.1364) |
| catholic husb. | 0.1754** | (0.0890) | -0.1144 | (0.0921) |
| religion, diff. | 0.1183 | (0.0813) | 0.1951** | (0.0783) |
| high sch., husb. | $-0.3956^{* * *}$ | (0.1153) | $-0.2602^{* *}$ | (0.1192) |
| college, husb. | $-0.5210^{* * *}$ | (0.1187) | $-0.5141^{* * *}$ | (0.1203) |
| education, diff. | 0.1240 | (0.0805) | 0.1816** | (0.0799) |
| avail. ratio, husb. | 0.7545*** | (0.2710) | 0.4834* | (0.2891) |
| avail. ratio, wife | -0.4683 | (0.3620) | 0.5872* | (0.3480) |
| separation, $\leq 1$ year | -0.2101* | (0.1085) | $-0.1190$ | (0.1031) |
| separation, > 1 year | 0.0137 | (0.0850) | $-0.2052^{* *}$ | (0.0859) |
| collection rate | $1.2183 * * *$ | (0.4120) | 0.0897 | (0.3968) |

${ }^{*},{ }^{* *}$, and ${ }^{* * *}$ denote significance at 10,5 , and 1 percent levels.

